

Complete this checkpoint on your own, and email your solution to okahn & afrank@andrew.cmu.edu by 11:59 PM on February 6th with “[FLAC checkpoint 1]” in the subject.

Your work should be legible and preferably typed, but you don’t have to use TeX.

## 1 CFGs

Make context-free grammars for the following languages:

- (a) Matched parentheses
- (b)  $\{w \in \{a, b, c\}^* \mid |w| \equiv 0 \pmod{2} \text{ or } |w| \equiv 0 \pmod{3}\}$
- (c)  $\{a^i b^j c^k \mid i = j \text{ or } j = k\}$

## 2 Ambiguity

What does it mean for a grammar to be ambiguous?

When might you want to avoid using an ambiguous grammar?

## 3 CNF

Write the following grammars in Chomsky normal form:

- (a)  $A \rightarrow BAB \mid B \mid \epsilon$   
 $B \rightarrow 00 \mid \epsilon$
- (b)  $A \rightarrow BB \mid \epsilon$   
 $B \rightarrow AA \mid 0 \mid 1$

## 4 PDA

Draw a push-down automaton for the language  $\{0^n 1^{2n} \mid n \in \mathbb{N}\}$ .