## 15-122: Principles of Imperative Computation

## Lab 03: Loopty-loopty Loop <br> Tuesday January $23^{\text {rd }}$

Collaboration: In lab, we encourage collaboration and discussion as you work through the problems. These activities, like recitation, are meant to get you to review what we've learned, look at problems from a different perspective and allow you to ask questions about topics you don't understand. We encourage discussing problems with other students in this lab!

## Setup:

Download the lab handout and code from the course website https://cs.cmu.edu/ 15122/handout$\mathrm{s} /$ code, and move it to your private directory in your unix.qatar.cmu.edu machine. Following that create a directory, move the handout to it, and unzip the handout file by executing the following commands:

```
mkdir lab_03
% mv 03-handout.tgz lab_03
cd lab_03
% tar -xvf 03-handout.tgz
```

You should write your code for part (2.b) in a file, consecutive.c0, in the directory lab03. For (3.b), use palindrome.c0 in the same directory.

## Submission:

## Reasoning about reversing an array of integers

You will be constructing loop invariants for a function (which we wrote for you) that reverses an array. As you define these loop invariants, take care to ensure both the safety of any array accesses as well as the correctness of the function itself.

Important! Specification functions are often inefficient, so don't use them in the actual code. Only use them inside contracts!

You will need to use the specification function is_reversed in your loop invariants. Remember, a specification function is for use in contracts to make sure the function is correct.
Here is the function header of is_reversed:

```
bool is_reversed(int[] first, int[] last, int i, int n)
//@requires 0 <= n && n == \length(first) && n == \length(last);
//@requires 0 <= i && i <= n;
```

This function returns true if the first $i$ numbers in the array first are the reverse of the last $i$ numbers of the array last. Now, using this specification function, fill in the loop invariants for the function reverse below, which reverses an array of integers.

Hint: Look at how we use is_reversed inside the //@ensures clause, and make sure that when the loop terminates, you can prove that this postcondition holds.
(1.a) Complete the missing loop invariants.

```
int[] reverse(int[] A, int n)
//@requires n == \length(A);
//@ensures is_reversed(A, \result, n, n);
{
    int[] B = alloc_array(int, n);
    for (int i = 0; i < n; i++)
    //@loop_invariant ; // SAFETY
    //@loop_invariant _ ; // CORRECTNESS
    {
        B[n - i - 1] = A[i];
    }
    return B;
    }
```


## Improving an already existing algorithm

The TAs have been tasked by Iliano to write some c0 code which takes an array of integers and sees how many consecutive pairs of equal numbers there are in the array. They were given the following examples:

| 1 | 5 | 4 | 4 | 2 | 1 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | has 2 consecutive pairs: $(4,4)$ and $(1,1)$


| 2 | 1 | 1 | 1 | 1 | 2 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| has 3 consecutive pairs: $(1,1)$ three times |  |  |  |  |  |  |


| 6 | 4 | 5 | 4 | 5 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| has 0 consecutive pairs |  |  |  |  |  |  |

The best solution the TAs could come up with involved an inefficient algorithm using two for loops, one within the other. As you will see later on in the course, this makes their code run very slowly for large arrays. They are pretty sure it can be done with just one loop, but they need your help!
(2.a) They've put their algorithm inside a function aptly named num_consecutive_slow(A, n). You can assume that it is correct (they wrote good test cases). One thing to note is that n can be less than the length of $A$ if you just want to check the first $n$ items of $A$ for pairs.
Now, using num_consecutive_slow as a specification function, complete the loop definition for the faster algorithm in the function below, including the bounds on $i$ as well as any loop invariants needed. Again, use one invariant for safety and one for correctness.

```
int num_consecutive_fast(int[] A, int n)
//@requires 0 <= n && n <= \length(A);
//@ensures \result == num_consecutive_slow(A, n);
{
    if (n == 0) return ____
    //@assert n >= 1;
    int count = 0;
    for (int i = ; i < ; i++)
    //@loop_invariant __
        //@loop_invariant _;
        {
        }
        return
}
(2.b) Now open up consecutive.c0 and fill in the loop body there. Remember, use the loop invariants to guide the code you write. When ready, test your implementation as described next.

Note: use the provided to_arr function to help with your testing. It takes an integer and converts it to an array of integers based on the number's digits.
```

% coin -d consecutive.c0
--> num_consecutive_fast(to_arr(1544211), 7);
2 (int)
--> num_consecutive_fast(to_arr(2111120), 7);
3 (int)
--> num_consecutive_fast(to_arr(6454545), 7);
0 (int)

```

You can test your code by running
```

cc0 -d -x consecutive.c0 test-consecutive.c0

```

\section*{3pt}

Make sure your code passes this test to get credit!

\section*{Error: out of memory}

Uh-oh! The \(15-122\) supercomputer has just run out of memory! Now how will the TAs tackle their next challenge? For some extra credit, see if you can help them out!
An int array is palindrome if reading it from left to right and from right to left yields the same numbers. For example, \([1,2,3,2,1]\) is palindrome, but \([1,2,3,4,2]\) is not. For years, \(15-122\) has been determining palindromes by checking if A and reverse (A, n) have the same contents. However, this requires allocating a new array every time you want to check if an array is palindrome. Alas, because we ran out of memory, we need a more efficient solution.
(3.a) The header for the old palindrome function is given below. It checks if \(\mathrm{A}[\mathrm{i}, \mathrm{j})\) is a palindrome. It uses an inclusive bound on \(i\), but an exclusive bound on \(j\).
bool is_palindrome_old(int[] A, int i, int j)
//@requires \(0<=i \& \& i<=j\) \&\& \(j<=\backslash l e n g t h(A) ;\)
The TAs have again started you off by writing the function header and the loop below. Try and fill in the loop invariants using the specification function we provided above.

Hint: you are returning true at the end of the function, so you want the loop invariants to help you prove that is_palindrome_old (A, 0, n) is true when the loop exits normally.
Remember: labs are collaborative! If this is challenging, work with your neighbors!
```

bool is_palindrome(int[] A, int n)
//@requires 0 <= n \&\& n <= \length(A);
//@ensures \result == is_palindrome_old(A, 0, n);
{
for (int i = ; i < ; i++)
//@loop_invariant __
//@loop_invariant __;
{
...
}
return true;
}

```
(3.b) Again, using these loop invariants to guide you, open up palindrome.c0 and fill in the loop body there. When ready, test your implementation as follows:
```

% coin -d palindrome.c0
--> is_palindrome(to_arr(1221), 4);
true (bool)
--> is_palindrome(to_arr(122), 3);
false (bool)
--> is_palindrome(to_arr(9), 1);
true (bool)

```

You can test your code by running
```

cc0 -d -x palindrome.c0 test-palindrome.c0

```

Make sure your code passes this test to get the extra credit!```

