

Definition MunkTop.17.1: If $A \subseteq X$ then A is a *closed set* in (X, \mathcal{T}) if and only if (X, \mathcal{T}) is a topological space and $X \setminus A$ is open in (X, \mathcal{T}) .

Definition MunkTop.17.2: If (X, \mathcal{T}) is a topological space and $A \subseteq X$ then $A^\circ = \cup \{U \in \mathcal{T} : U \subseteq A\}$.

Definition MunkTop.17.3: If (X, \mathcal{T}) is a topological space and $A \subseteq X$ then \bar{A} is the intersection over the set of F such that $A \subseteq F$ and F is a closed set in (X, \mathcal{T}) .

Definition MunkTop.17.4: $A \cap B \neq \emptyset$ if and only if $A \cap B \neq \emptyset$.

Definition MunkTop.17.4.5: $A \cap B = \emptyset$ if and only if $A \cap B = \emptyset$.

Definition MunkTop.17.5: If (X, \mathcal{T}) is a topological space and $x \in X$ and $U \in \mathcal{T}$ then U is a *neighborhood* of x in (X, \mathcal{T}) if and only if $x \in U$.

Definition MunkTop.17.6: If (X, \mathcal{T}) is a topological space and $x \in X$ and $A \subseteq X$ then x is a *limit point* of A in (X, \mathcal{T}) if and only if for every U , if U is a neighborhood of x in (X, \mathcal{T}) then $U \cap A \setminus \{x\} \neq \emptyset$.

Definition MunkTop.17.7: If (X, \mathcal{T}) is a topological space and f is in the set of maps from \mathbb{N} to X and $x \in X$ then f *converges to* x under \mathcal{T} if and only if for every $U \in \mathcal{T}$, if U is a neighborhood of x in (X, \mathcal{T}) then there exists $N \in \mathbb{N}$ such that for every $n > N$, $f(n) \in U$.

Definition MunkTop.17.8: If (X, \mathcal{T}) is a topological space then (X, \mathcal{T}) is a *Hausdorff space* if and only if for every $x, y \in X$, if $x \neq y$ then there exist $U, V \in \mathcal{T}$ such that $x \in U$ and $y \in V$ and $U \cap V = \emptyset$.

Definition MunkTop.17.9: If (X, \mathcal{T}) is a Hausdorff space and there exists y such that f converges to y under \mathcal{T} then x is a *limit* of f if and only if x equals the unique y such that f converges to y under \mathcal{T} .