

Interactive Preference Measurement for Consumer Decision Support

John Liechty Srikant Vadali Arvind Rangaswamy Penn State University

June 7, 2004





Our Corporate Sponsors: IBM, Unisys, Xerox, AT&T Wireless, Delphi Ventures, SAP America, Cigna, Tyco International, HP

© Pennsylvania State University 2004



- Decision Theory Framework: Objective Function, Individual Level Utility
 - Recommend 'best' product
- Need an Individual Utility Function
 - Attribute based product space
 - Specifically understand high utility region
- Data: Experimental Sequence of Questions
- Timing: Real-time processing



Helping Customers Make Good Choices in Crowded Markets

Consumers face an increasing array of choices:

- Over 8,200 mutual funds
- Over 500 models of cars
- Over 30,000 products in a grocery store
- Over 100,000 prescription drugs



Choosing is not so Easy!



🕲 Active Buyer's Guide -	Netscape			$\mathbf{ imes}$
Eile Edit View Go Bookr	narks <u>T</u> ools <u>W</u> indow <u>H</u> elp			
Active Buver's Guide				
Active Sales Assista	personalized product recomm from smart virtual sales assist	endations ants.		e N S
SHOPPERS These virtual sales assistants give you the best product recommendations based on your preferences, for free. You get: Recommendations ranked from best fit to worst, plus prices from leading retailers. Image: Toshiba SD-275 Image: Recommendations ranked from best fit to worst, plus prices from leading retailers. Image: Recommendations ranked from best fit to worst, plus prices from leading retailers. Image: Recommendations ranked from best fit to worst, plus prices from leading retailers. Image: Recommendations ranked from best fit to worst, plus prices from leading retailers. Image: Recommendations ranked from best fit to worst, plus prices from leading retailers. Image: Recommendations ranked from best fit to worst, plus prices from leading retailers. Image: Recommendations ranked from best fit to worst, plus prices from leading retailers. Image: Recommendations ranked from best fit to worst, plus prices from leading retailers. Image: Recommendations ranked from best fit to worst, plus prices from leading ranked from best fit to worst, plus prices from leading ranked from best fit to worst, plus prices from ranked from best fit to worst, plus prices from leading ranked from best fit to worst, plus prices from leading ranked from best fit to worst, plus prices from ranked from best fit to worst, plus prices from ranked from best fit to worst, plus prices from leading ranked from best fit to worst, plus prices from ranked from best fit to worst, plus prices from ranked from best fit to worst, plus prices from ranked from best fit to worst, plus prices from thestreaked fro	Search or choose a Appliances Refrigerators, Dishwashers, Washers, Drvers, Microwave Ovens, Cordless Phones, Corded Phones, More Cameras Digital Cameras, Point and Shoot Cameras, SLR Cameras Electronics MP3 Plavers, Projection TVs, Camcorders, DVD Plavers, Personal Video Recorders, Minisystems, Plasma Displays, Home Theater Systems, CD Plavers, More Computer Products Monitors, Notebook Computers, Inkiet Printers, PDA/Handhelds, Laser Printers, Desktop Computers, Digital Cameras, More Copyright © 2002 Active Decisions Inc. All rights reserved about privacy terms and conditions	category below Family & Lifestyle Cats. Dogs. Vacation Destinations Home & Garden Cordless Phones. Corded Phones. Coffee/E Maters. Dryers. Washers. Washer/Dryer Corr Office Machines Multimedia Projectors. Laser Printers. Inkie Mobile Phones Sports & Recreation Global Positioning Systems, Vacation Dest by	Active Sales Assistant: An example commercial service that helps customers makes choices in an online environment. www.activebuyersguide.com	

🕲 Active Buyer's Guide: D	igital Cameras - Netscape		
_ <u>F</u> ile <u>E</u> dit ⊻iew <u>G</u> o <u>B</u> ookn	arks <u>T</u> ools <u>W</u> indow <u>H</u> elp		
📔 💊 Active Buyer's Guide: D	gital Cameras		
Active Sales Assista	personalized product recommendations from smart virtual sales assistants.		
SHOPPERS			
These virtual sales assistants give you the best product recommendations based on your preferences, for free.			
You get: Recommendations ranked from best fit to worst, plus prices from leading retailers	Digital Cameras Guide		
1 Toshiba SD-275 2 3 Onkyo DV-S555 3 Sony DVP-F21	Need help deciding which Digital Camera to buy? Get highly personalized and completely unbiased product recommendations with our decision guide!	Full Product Specs Pictures & Reviews Side-by-Side Compare Where-to-buy links	
BUSINESSES	choose a search method		
Increase sales on your site with Active Sales Assistant! Our clients typically double their sales conversion rates	Power Search Get recommendations quickly based on your price, brand,	and feature preferences.	
Free report	Get Advice Get recommendations based on how you intend to use yo	ur digital cameras.	
the top 5 secrets to great online selling	Decision Guide Get recommendations by making trade-offs between price	brand, and features.	
A site without Active Sales Assistant is like a store without sales people.	you can also <u>read buying tips</u>		
» <u>learn more</u> » <u>contact us today</u>	Copyright © 2002 Active Decisions Inc. All rights reserved. <u>about</u> <u>privacy</u> <u>terms and conditions</u>		

🕸 Active Buyer's Guide - N	letscape	
Eile Edit View Go Bookm	arks <u>T</u> ools <u>W</u> indow <u>H</u> elp	
Active Buyer's Guide		
Active Sales Assista	nt personalized product recommendations from smart virtual sales assistants.	
SHOPPERS		
These virtual sales assistants give you the best product recommendations based on your preferences, for free.		
You get: Recommendations		
plus prices from leading	Digital Cameras FEATURES GLOSSARY	
retailers.	steps: 1 Price & Features 2 Settings 3 Brands 4 Tradeoffs 5 Fine Tune 6 Profile > RESULTS	
2 4 Onkyo DV-S555	What is the most you are willing to pay for a Digital Camera?	
3 Sony DVP-F21	min \$ 0 max \$ 400 show price range	
BUSINESSES	(optional) (required) Which features do you care about?	
Increase sales on your site	tip: click any feature for description	
With Active Sales Assistant! Our clients typically double	Image Capacity (at histes)	
their sales conversion rates.	Number of hi-res pics stored in the memory Number of pixels in an image; more pixels = provided sharper picture	
Eree report	Plays MP3s Rapid-Fire Shots	
the top 5 secrets	Allows for multiple shots w/one touch of the button	
to great online selling	Camera Size Ease of Download How the camera downloads pics to your computer/printer	
Assistant is like a store without sales people.	Flash Type Options for flash, such as auto, hot shoe, flash sync	
» <u>learn more</u> » <u>contact us today</u>	Delay Between Shots How long the camera takes to process & store an image	
	5 steps to go Next >>	
	Copyright © 2002 Active Decisions Inc. All rights reserved. about privacy terms and conditions	

🕲 Active Buyer's Guide - 1	letscape	
🔺 <u>F</u> ile <u>E</u> dit <u>V</u> iew <u>G</u> o <u>B</u> ookm	arks <u>T</u> ools <u>W</u> indow <u>H</u> elp	
Active Buyer's Guide		<u> </u>
Active Sales Assista	nt ^{**} personalized product recommendations from smart virtual sales assistants.	
SHOPPERS		
These virtual sales assistants give you the best product recommendations based on your preferences, for free.		
You get: Recommendations		
ranked from best fit to worst, plus prices from leading	Digital Cameras FEATURES GLOSSARY	
retailers.	steps: 1 Price & Features 2 Settings 3 Brands 4 Tradeoffs 5 Fine Tune 6 Profile > RESULTS	
1 Toshiba SD-275		
3 Sony DVP-F21	Tou do not have to answer every item below, only those that you care about.	
BUCKUEGOEG	Do you have any minimum or maximum requirements?	
BUSINESSES	Image Capacity (at hi-res) Resolution	
with Active Sales Assistant!	10 at least 🔽 1600 x 1200 pixels at least 💌	
their sales conversion		
rates.	lan derinder en their feature to mu?	
Free report		
the top 5 secrets	Flash Type Never (desirable) Must	
to great online selling	None CCCCCCC	
A site without Active Sales		
Assistant is like a store without sales people.	Flash Sync CCCCCC	
	Hot Shoe CCCCC	
» <u>learn more</u>		
» <u>contact us today</u>	Compared to each other, how important is each feature?	
	tip: click any feature for description	
	Resolution CCCCCC	
	Brand CCCCCC	
	Image Capacity (at hi-res) C C C C C C	
	Price CCCCCC	
	Flash Type C C C C C	
	4 steps to go Next >>	

Active Buyer's Guide - N	Vetscape			📃 🗖 🔀
<u>_</u> Eile <u>E</u> dit <u>V</u> iew <u>G</u> o <u>B</u> ookm	arks <u>T</u> ools <u>W</u> indow <u>H</u> elp			
b				
🖓 🛇 Active Buver's Guide				X
Active Sales Assista	nt [™] personalize from smart	d product recommendations virtual sales assistants.		powered by DECISIONS
SHOPPERS				
These virtual sales assistants give you the best product recommendations based on your preferences, for free.				
You get: Recommendations ranked from best fit to worst,	Digital Cameras		FEATURES LALOSSARY	
plus prices from leading	Digital Cameras	and the second	FEATURES OLUSSART	
1 Toshiba SD-275 2 S Onkyo DV-S555 3 Sony DVP-F21	steps: 1 Price & Features How desirable are these t "Never Buy" will eliminate	2 Settings 3 Brands 4 Tradeoffs rands to you? that brand from your results	5 Fine Tune 6 Profile > RESULTS	Ξ
BUSINESSES		Never (desirable) Buy < less more >		
Increase sales on your site	Achiever	222222		
with Active Sales Assistant! Our clients tunically double	AGFA	229222		
their sales conversion	Aiptek	00000		
rates.	Aiwa	00000		
	Alpha Vision Tech	00000		
Free report	Argus	00000		
the top 5 secrets	Bell & Howell	0 0 0 0 0 0		
to great online selling	BenQ	0 0 0 0 0 0		
	Canon	<u> </u>		
A site without Active Sales	Casio	<u> </u>		
Assistant is like a store without sales people	Concord Cameras			
suice people.	Contax			
» learn more	Creative Labs			
» contact us today	Costal Digital	0 0 0 0 0 0		
" Condector today	Delta	0 0 0 0 0 0		
	Dolphin Peripherals	0 0 0 0 0 0		
	Epson	0 0 0 0 0 0		
	Ezonics	0 0 0 0 0 0		
	Fujifilm	2 2 2 2 2 2		
	Hewlett Packard	229222		
	Intel	229222		
	JVC	0 0 0 0 0 0		
	KB Gear	00000		
	Kodak	00000		
	Konica	00000		
	Kyocera	0 0 0 0 0 0		
	Largan	229222		
💟 🛀 🧏 🖭 Docume	nt: Done (5.531 secs)			

🕲 Active Buyer's Guide -	Netscape		
Eile Edit View Go Bookn	narks <u>T</u> ools <u>W</u> indow <u>H</u> elp		
🕙 🛇 Active Buyer's Guide			×
Active Sales Assista	personalized product recommendations from smart virtual sales assistants.	power b	
SHOPPERS			
These virtual sales assistants give you the best product recommendations based on your preferences, for free.			
You get: Recommendations			
ranked from best fit to worst, plus prices from leading			
retailers.	Digital Cameras	FEATURES GLOSSARY	
1 P Toshiba SD-275 2 2 Onkyo DV-S555	steps: 1 Price & Features 2 Settings 3 Brands 4 Tradeoffs 3 Fine	Tune b Profile > RESULTS	
3 Sony DVP-F21			
	Assuming all other features are the same, which product do you pr	efer?	
Increase sales on your site	Click (1) for definition		
with Active Sales Assistant!	Digital Camera A	Digital Camera B	
their sales conversion			
rates.	i) 20 images at hi-res prefer more prefer more	i) 50 images at hi-res	
Free report	ວັດວ່າວ່າວ່າ		
the top 5 secrets	(i) \$200	i) \$300	
to great online sening			
A site without Active Sales			
sales people.	For best results, the to 4 tradi	eoff questions	
» learn more			
» contact us today	Copyright © 2002 Active Decisions Inc. All rights reserved.	powered Active	
	Server prosect tenne and constanting	DECISIONS	

🕲 Active Buyer's Guide - N	letscape				
🔺 Eile Edit <u>V</u> iew <u>G</u> o Bookm	arks <u>T</u> ools <u>W</u> indow <u>H</u> elp				
Active Drugevic Cuide					
Active Sales Assista	nt [™] personalized from smart vi	product recommendation: tual sales assistants.	S		by Active
SHOPPERS					
These virtual sales assistants give you the best product recommendations based on your preferences, for free.					
You get: Recommendations ranked from best fit to worst,					
plus prices from leading	Digital Cameras		<u>FEA</u>	TURES GLOSSARY	
1 Toshiba SD-275 2 Sony DV-555 3 Sony DVP-F21	steps: 1 Price & Features 2 How likely would you purcha This step fine tunes your results	Settings 3 Brands 4 Tradeo se these example products? by calculating how well existing	ffs 5 Fine Tune 6 Pi products fit your needs.	rofile > RESULTS	
BUSINESSES		Example A	Example B	Example C	
Increase sales on your site	Brand	Fujifilm	Oregon Scientific	Achiever	
with Active Sales Assistant!	Price	\$343.96	\$300	\$100	
their sales conversion rates.	<u>Flash Type</u>	Flash Sync, Hot Shoe, Red-Eye Reduction, Off/On/Auto	Hot Shoe,None	Hot Shoe,None	
	Image Capacity (at hi-res)	20	50	50	
Free report	Resolution	1600×1200 pixels	2048 x 1536 pixels	2560 × 1920 pixels	
to great online selling	Answer all 3 >	Definite	💽 Likely 💽	Unlikely 🗾	
A site without Active Sales Assistant is like a store without sales people.			1 step to	go Next>>	
» <u>learn more</u> » <u>contact us today</u>	Copyright © 2002 Active Decisions <u>about</u> <u>privacy</u> <u>terms and conc</u>	: Inc. All rights reserved. Iitions	poy		

Active Buyer's Guide - N	Netscape							
Eile Edit View Go Bookm	arks <u>T</u> ools	<u>W</u> indow <u>H</u> elp						
🕘 🛇 Active Buyer's Guide								X
Active Sales Assista	nt™	personali from sma	zed product recommenda rt virtual sales assistants.	itions				
SHOPPERS	Digital	Cameras			FEA	TURES GLOSSAR	<u>Y</u>	
These virtual sales assistants give you the best product recommendations based on	r	esults					_	
your preferences, for free.	sorted by	: RANK	🗾 🔷 sort directio	n e	xpand list	to: 5 results 👱	-	
You get: Recommendations ranked from best fit to worst,	rank 🔻		Brand & Model		avg. street price	Compare		
retailers.	1	Fujifilm FinePix: 20 images at hi Red-Eye Reduc 1200 pixels Res cable, Downloa - 0.8 sec Dela MP3s	30) 💼 res - Flash Sync Flash Type, Hot tion Flash Type, Off/On/Auto Flash olution - 2.5X Optical Zoom - I d via removable memory - 5 Rap y Between Shots - Pocket Camer	t Shoe Flash Type, n Type - 1600 x Download via USB pid-Fire Shots ra Size - Plays	\$343.96 US	WHERE TO BUY compar	re	
BUSINESSES		more features						_
Increase sales on your site with Active Sales Assistant Our clients typically double their sales conversion rates. Free report the top 5 secrets	2	Minolta Dimage 10 images at hi Flash Type, Off, Resolution - 4 Download via re Delay Between MP3s more features	S304 6 res - Hot Shoe Flash Type, Red- 'On/Auto Flash Type - 2048 × 15 X Optical Zoom - Download via movable memory - 9 Rapid-Fire Shots - Medium Camera Size -	Eye Reduction 36 pixels USB cable, Shots - 3 sec Does Not Play	\$459.85 US	WHERE Compar	re	
to great online selling		Sony Cyber-sho	EDSC-P31 💼					
A site without Active Sales Assistant is like a store without sales people. » <u>learn more</u>	3	118 images at f Flash Type - 1 - Download vi Between Shots more features	i-res - Red-Eye Reduction Flash 600 x 1200 pixels Resolution - 1 a USB cable - 16 Rapid-Fire Sho - Medium Camera Size - Does	<mark>Type, Off/On/Auto</mark> IX Optical Zoom hts - 2 sec Delay Not Play MP3s	\$220.00 US	WHERE Compar	re	
» <u>contact us today</u>		Flash Type : Mu	ist Have Hot Shoe					
		Ezonics VistaC/ 12 images at hi pixels Resolutio Download via re	M. Echo (a) res - Off/On/Auto Flash Type - n - OX Optical Zoom - Downloa movable memory - 5 Rapid-Fire	2048 x 1536 ad via USB cable, Shots - 2 sec	¢105 37			
	4	Delay Between MP3s <u>more features</u> *not accepta	Shots - Pocket Camera Size - (ble because you said:	Does Not Play	φ105.27 US	TO BUY compar	re	
		<u>Vivitar ViviCam</u> 18 images at hi	3695 C	ype, Off/On/Auto			_	
🔊 🖂 🤱 🞯 🔲 Docume	nt: Done (2.26	 Download vi 6 secs) 	a IISB cable . 3 Ranid-Eire Shot	s . 4 sec Delay	¢100.05			

BRCC More Headaches for Customers!



Desirable Characteristics of Simplified Preference Assessment Methods

- Interactive
- Adaptive
- Focused/brief
- Real-time (< 5 seconds response latency)
- Share information across customers
- Have memory of past purchases of customer
- Useability
- Generate customer confidence

Ex ante conjoint model building

Dialog at Web site

- <u>Study 1</u>: Sequential questioning to minimize predictive error around the most desirable option.
- <u>Study 2</u>: Making recommendations to impatient customers using demographic information.
- <u>Study 3</u>: Probabilistic fast polyhedral: Estimation and sequential design.

Study 1: Ratings and the Predictive Error

© Pennsylvania State University 2004

Study 1: Ratings and the Predictive Error

Model Development

Strategy for sequential questions:

i. Predictive error minimization

Ex ante conjoint model building

Predictive Squared Error Loss Function

$$L_{n+1} = (y_{n+1} - c^T \beta_{n+1})^2$$

- y_{n+1} : next rating to be given
 - *c* : element of design space (a product profile)
- β_{n+1} : next estimate of partworths

Preposterior risk

$$R_{n+1} = E_{y_{n+1},\beta_{n+1}|D_n,X_{n+1},c} [L_{n+1}]$$

 X_{n+1} : next profile to be rated (decision task at hand)

$$D_n = \{X_1, ..., X_n, y_1, ..., y_n\}$$

Predictive Distribution

$$y_{n+1} | X_{n+1}, \beta_{n+1} =_d N(X_{n+1}^T \beta_{n+1}, \sigma^2)$$

Prior

$$\beta_{n+1} | D_n, \beta_0, \Sigma, \sigma^2 =_d N(B^{-1}b, B^{-1})$$

$$B^{-1} = \Sigma^{-1} + \frac{1}{\sigma^2} \sum_{i=1}^n X_i X_i^T \qquad b = \Sigma^{-1} \beta_0 + \frac{1}{\sigma^2} \sum_{i=1}^n X_i y_i$$
$$\beta_1 =_d N(\beta_0, \Sigma) \quad : \text{ informative starting prior}$$

Minimizing preposterior risk

$$R_{n+1} = E_{y_{n+1,\beta_{n+1}|D_n,X_{n+1},c}} [L_{n+1}]$$

$$R_{n+1} = \sigma^{2} + (X_{n+1} - c)^{T} \underbrace{(\Sigma^{-1} + \beta_{n} \beta_{n}^{T})}_{\text{positive}} (X_{n+1} - c)$$

 $X_{n+1} = c$: minimizes preposterior risk

What part of the design space does the decision maker care about?

Minimizing risk based on what is important to the individual:

$\mu_n(c)$:density on design space reflects areas of interest to decision maker

Ω :design space, set of possible products

Minimizing expected risk based on what is important to the individual:

$$\min_{X_{n+1}\in\Omega} E_{\mu}[R_{n+1}] = E_{\mu}[R_{n+1} | X_{n+1} = E_{\mu}[c]]$$

Possible densities

1. Singleton: mass on design point with largest utility

2. Proportional: mass proportional to utility

Possible densities

1. Singleton: mass on design point with largest utility $\mu_n(c) = I \left\{ c^T \beta_n = \max_{c^* \in \Omega} \left\{ c^{*T} \beta \right\} \right\}$

2. Proportional: mass proportional to utility

$$\mathcal{U}_{n}(c) \propto c^{T} \beta_{n} I\{c \in \Omega\}$$
$$-\min_{c^{*} \in \Omega} \{c^{*T} \beta_{n}\} I\{\min_{c^{*} \in \Omega} \{c^{*T} \beta_{n}\} < 0\}$$

CERCE Study 1: Ratings and the Predictive Error

(sample)

Model Development

- Strategy for sequential questions:
- i. Predictive error minimization

Prior Measurement And Analysis

- Obtain data either from a survey or past purchases.
- Generate prior distribution for model.

Chinese Dinner Study

Ex ante conjoint model building

- Study context:
 - Chinese Dinners
 - 8 attributes, 2, 3, or 4 options each
 - 4 profiles for predictive validation
- Phase I -- Obtain Prior Distribution: β_0, Σ
 - 24 subjects
 - 27 profiles to rate (Orthogonal design)

Study 1: Ratings and the Predictive Error

- Phase II Dynamic Approach
 - 20 students
 - Dynamically generated product profiles using singleton density

Study 1: Ratings and the Predictive Error Software Implementation

© Pennsylvania State University 2004

Welcome to the questionairre hosting service	from mktgeng.com - Microsoft Internet Explorer	
<u>F</u> ile <u>E</u> dit <u>V</u> iew F <u>a</u> vorites <u>T</u> ools <u>H</u> elp		an a
🚱 Back 🝷 🕥 👻 🗾 🛃 🏠 🔎 Search	📌 Favorites 🜒 Media 🧭 🔗 - 🌺 🕼 -	
Address 🗃 http://software.mktgeng.com:81/aca-conjoint/cl	ean/cjlogin.html	🕑 🄁 Go 🛛 Links 🎽
	Welcome to conjoint analysis from mktgeng.com	
	Please Enter Your E-mail Id arvindr@psu.edu	
If	Please enter any special id given to you `no special id was provided, you may leave this field blank test	
	Enter	

Instructions

In this section, you will be presented with a set of product attributes as part of a product rating task. Each product attribute has a number of options. For example, in a study of cars, the product attributes of interest might be price, color, type of engine and the options for color might be red, blue, and white.

First, for each product attribute, you will be asked to select the option that you prefer the most. Next you will be asked to rate the remaining options for that attribute on a scale from 0 to 10 to represent how much you prefer each option. A high rating score indicates that you have greater preference for that option. For example, if you prefer an option almost as much as your most preferred option, you should give it a score close to 10. If your preference

Continue >>

🚰 Please distribute 100 points among the following attributes - Microsoft Internet Explorer	
<u>F</u> ile <u>E</u> dit <u>V</u> iew F <u>a</u> vorites <u>T</u> ools <u>H</u> elp	A.
🕞 Back 🝷 🕥 - 💽 🛃 🏠 🔎 Search 👷 Favorites 🔇 Media 🚱 😒 🖓 -	
Address 🕘 http://software.mktgeng.com:81/aca-conjoint/clean/cjlogin.pl	💙 🔁 Go 🛛 Links 🎽

Please distribute 100 points among the following product attributes. You should give higher number of points to those attributes which are more important to you when deciding on a Chinese dinner. Note that the points should sum to 100.

Soup:	0
Rice/Noodle:	0
Sauce:	0
Vegetables:	0
Meat:	0
Spring Roll:	0
Quantity:	0
Price:	0

Continue >>

Continue >>

- Expectations
 - Profiles being rated have a higher preferred score, on average, as number of profiles rated increases
 - Calculate average rating, across all participants, each time a profile was rated

$$\overline{y}_n = \sum_{i=1}^{IND} \frac{y_{i,n}}{IND}$$

- Expectations
 - Profiles being rated have a higher preferred score, on average, as number of profiles rated increases
 - Ability to forecast rating of most preferred profile increases over time (MSE gets smaller)
 - Consider how well dynamic estimates predict the rating of the last profile
 - Calculate MSE for last profile (across all participants) based on dynamic estimates of partworths

$$MSE_n = \frac{1}{IND} \sum_{i=1}^{IND} \left(y_{i,N} - \beta_n^T X_{i,N} \right)^2$$

- Expectations
 - Profiles being rated have a higher preferred score, on average, as number of profiles rated increases
 - Ability to forecast rating of most preferred profile increases over time (MSE gets smaller)
 - Ability to forecast over other parts of the design space decreases over time (MSE gets larger)
 - Calculate the MSE (across all participants) for the hold-out profiles, based on dynamic estimates

IND $\left(y_{i,N}^{T}-\beta_{n}^{T}X_{i,N}\right)$ MSE_n IND *i*=1

Study 3: Probabilistic Fast Polyhedral Model

© Pennsylvania State University 2004

Study 3: Probabilistic Fast Polyhedral Model

Model Development

Strategy for sequential questions: iii. Probabilistic fast polyhedral

Ex ante conjoint model building

Study 3: Motivation

- Polyhedral Approaches for Conjoint Analysis (Toubia et al. Marketing Science, 2003).
 - Question sequence & Estimation of partworth utilities
- Key idea:
 - Represent feasible values of partworths as a bounded polyhedron.
 - Reduce polyhedron rapidly with 'optimal' questions.
 - 'Center' of polyhedron is the partworth estimate.
- However, response errors (i.e., responses that lead to infeasible regions) are treated in a theoretically appealing manner.
- Our aim: Extend polyhedral method to incorporate response error using a well-defined probability model.

EXAMPLE 7 Study 3:FASTPACE: Two-attribute Laptop Example

Ask respondent:

How much do you prefer product 1 over product 2?

- Set least desirable level of attributes to 0.
- Each response results in a reduction of the dimensionality of the polyhedron.

• Ask another question and refine our estimates.

• Response error is allowed only when inconsistent responses are detected.

Study 3: Extending FASTPACE

• Incorporate response error within FASTPACE framework using a general probability model.

EBRC

- After next question, the space shrinks further.
- Procedure ensures that there is always some probability mass in the feasible region.

• Enhanced HB Regression Framework

 $a_i \sim N(X_i\beta_i, \sigma^2) I(X_i\beta_i - \delta\sigma 1 < a_i < X\beta_i + \delta\sigma 1)$

• Probability Model for the parameters

 $\beta_i \sim N(\overline{\beta}, \Sigma) I(\beta_i \ge 0) I(\sum \beta_i \le 100)$

 $\sigma^2 \sim IG(shape, scale)$

• Assume prior distributions for $\overline{\beta} \sim N(.,.), \Sigma \sim IW(.,.)$

- Initial test of model done using laptop bag study of Toubia et al (2003).
- Details:
 - 88 respondents.
 - Respondent answered self-explicated questions followed by 20 paired comparison questions.
 - Each paired comparison question had product descriptions consisting of 3 attributes that were chosen from 10 attributes.
 - Each attribute had 2 levels.
- Hold-out task: Respondents rank-ordered 5 bags (selected randomly out of 16 available bags).
- Goal of test: To examine how well FASTPACE and our model predict the ranking of the bags.

- Preliminary results show that our model performs on par with FASTPACE on holdout task (their laptop bags data).
- Our rank order correlation with actual choice: 0.68
- FASTPACE rank order correlation: 0.68
- Their Sawtooth software HB model's rank order correlation: 0.64

- Implement question design
 - FASTPACE based on structure of polyhedron.
 - Our approach: Based on probability model.
- Fully nest FASTPACE within our HB model
 - Currently, FASTPACE is conceptually nested within our model.
 - However, operationally, FASTPACE uses min-max criteria whereas we use min sum of squared errors criteria (i.e., OLS-type minimization).
- Develop implementation techniques for question sequencing and estimation in real-time web environments.

- We extend FASTPACE by incorporating response errors in a theoretically appealing manner.
- With test data (and without full nesting of FASTPACE within our approach), HB does as well as FASTPACE.
- Further research in progress to establish domains of applicability of our HB model (especially with reference to FASTPACE).

Your thoughts/suggestions for future research?