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## Valuing Customers

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## Customers as Assets

- “A widening consensus is growing that the importance of (intangible) assets – from brand names and customer lists ...-- means that investors need to know more about them. A task force appointed by SEC will encourage companies to provide more information regarding those assets.”  
- New York Times, May 22, 2001
  - “The world is coming our way.” J.D.C. Little
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## Overview

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- RFM Models
  - Simple models of LTV
  - Antecedents of LTV
  - From customer value to firm value
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## RFM Models

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- Scoring models
    - Aaker, Kumar and Day (1998)
    - Hughes (2000)
  - Predictive models
    - AID, CHAID, CART, Discriminant Analysis
    - Colombo and Jiang (1999)
    - Bult and Wansbeek (1995)
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## From RFM to LTV

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- Spreadsheet approach (Reichheld 1996, Blattberg & Deighton 1996)

Margin		$m_1$	$m_2$	$m_3$	...	$m_t$
Retention		$r_1$	$r_1 r_2$	$r_1 r_2 r_3$	...	$r_1 r_2 r_3 \dots r_t$
Number of Customers	$n_0$	$n_1$	$n_2$	$n_3$	...	$n_t$
Acquisition Cost	$AC_0$	$AC_1$	$AC_2$	$AC_2$	...	$AC_t$
Discount	1	$1/(1+i)$	$1/(1+i)^2$	$1/(1+i)^3$	...	$1/(1+i)^t$

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## Simple Models of LTV

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- Constant margin, 100% retention

$$LTV = \frac{m}{(1+i)} + \frac{m}{(1+i)^2} + \dots = \int_0^{\infty} m e^{-it} dt = \frac{m}{i}$$

- Constant margin, retention  $r$

$$LTV = \frac{mr}{(1+i)} + \frac{mr^2}{(1+i)^2} + \dots = \int_0^{\infty} m e^{-\left(\frac{1+i-r}{r}\right)t} dt = m \frac{r}{1+i-r}$$

Berger and Nasr (1998)  
Gupta and Lehmann (2001)

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## Margin Multiple

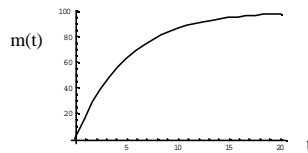
$$\frac{r}{1+i-r}$$

Retention Rate	Discount Rate			
	10%	12%	14%	16%
60%	1.20	1.15	1.11	1.07
70%	1.75	1.67	1.59	1.52
80%	2.67	2.50	2.35	2.22
90%	4.50	4.09	3.75	3.46

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## Simple Models of LTV

- Concave function for margin, constant retention  $r$



$$m(t) = a(1 - e^{-bt})$$

$$LTV = \int_0^{\infty} m(t) e^{-\left(\frac{1+i-r}{r}\right)t} dt = \frac{abr^2}{(1+i-r)(1+i-r(1-b))}$$

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## Antecedants of LTV

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- **Service quality**
  - Negative evidence
    - McKinsey & Co (1992), A.T. Kearney (1992), Arthur D. Little (1992)
  - Positive evidence
    - Aaker & Jacobson (1994), Hendrick & Singhal (1997), Easton & Jarrell (1998)
- **Satisfaction**
  - Empirical: Anderson, Fornell and Lehmann (1994)
  - Analytical: Hauser, Simester & Wernerfelt (1995)

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## Antecedants of LTV

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- **Duration of stay and retention**
  - Positive evidence: Reichheld (1996)
  - Negative evidence: Reinartz & Kumar (2000)
- **Modeling retention**
  - Hazard models (Helsen & Schmittlein 1993)
  - Stochastic models (Schmittlein, Morrison & Colombo 1987)
- **Loyalty and loyalty programs**
  - Loyalty programs work: Dreze & Hoch (1998)
  - Loyalty programs don't work: Sharp & Sharp (1997), Dowlings & Uncles (1997)

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## Antecedants of LTV

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- When do loyalty program work?
  - Convex relation between reward and usage (Kivetz 2000)
  - Exploit principal agent
  - Psychological principles work (Kivetz and Simonson 2001)
- Lessons from Economic Theory
  - Price competition effect (Chen 1997, Fudenberg & Tirole 2000)
  - No Prisoner's dilemma (Shaffer & Zhang 2001, Nalebuff 2001)
  - Imperfect targetability effect (Chen, Narasimhan and Zhang 2001)
  - Acquisition or retention (Fudenberg & Tirole 2000, Shaffer & Zhang 2000)
  - When customers focus on future benefits (Koppalle, Neslin and Singh 2001)
  - When category expands (Koppalle, Neslin and Singh 2001)

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## From Customer Value to Firm Value

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- Valuation for Internet companies difficult
- Traditional methods and their modifications
  - Damodaran (2001)
- Wall Street's "innovations"
- Accounting approaches
  - Trueman, Wong & Zhang (2001), Hand (2000)

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## Valuing Customers

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- Value = Benefit - Cost

$$= f_1(n_t, m_t, i, r) - f_2(n_t, c_t, i)$$

Gupta, Lehmann and Stuart (2001)

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## The Benefit

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- Number of customers, margin and benefit at each time period will be

Time 1	$n_1 r$				$m_1$
2	$n_1 r^2$	$n_2 r$			$m_2$
3	$n_1 r^3$	$n_2 r^2$	$n_3 r$		$m_3$
4	$n_1 r^4$	$n_2 r^3$	$n_3 r^2$	$n_4 r$	$m_4$
·	↓		↘		·

$$n_1 \left[ \frac{m_1 r}{(1+i)} + \frac{m_2 r^2}{(1+i)^2} + \dots \right] \quad n_2 \left[ \frac{m_2 r}{(1+i)^2} + \frac{m_3 r^2}{(1+i)^3} \dots \right]$$

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## The Benefit

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- In general,

$$Benefit = \sum_{k=0}^{\infty} \sum_{t=k}^{\infty} n_k \frac{m_t r^{(t-k)}}{(1+i)^t}$$

- In continuous time we have

$$Benefit = \int_{k=0}^{\infty} \int_{t=k}^{\infty} n(t)m(t)e^{-\left(\frac{1+i-r}{r}\right)t} dt dk$$

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## The Cost

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- Similarly the acquisition cost is

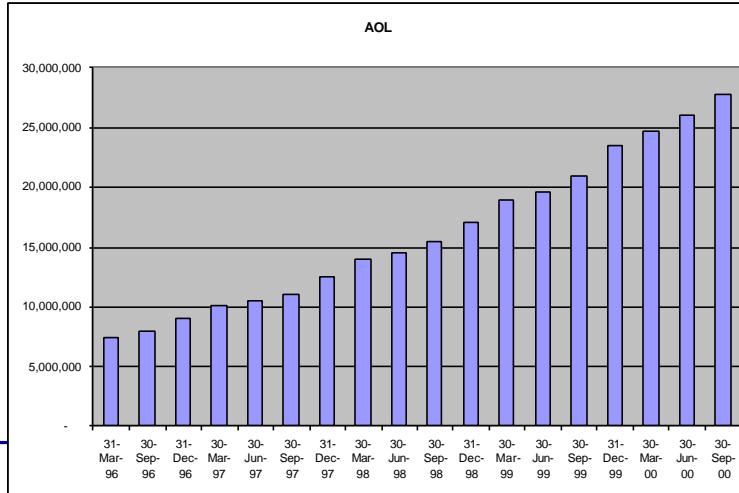
$$Cost = \int_{t=0}^{\infty} n(t)c(t)e^{-it} dt$$

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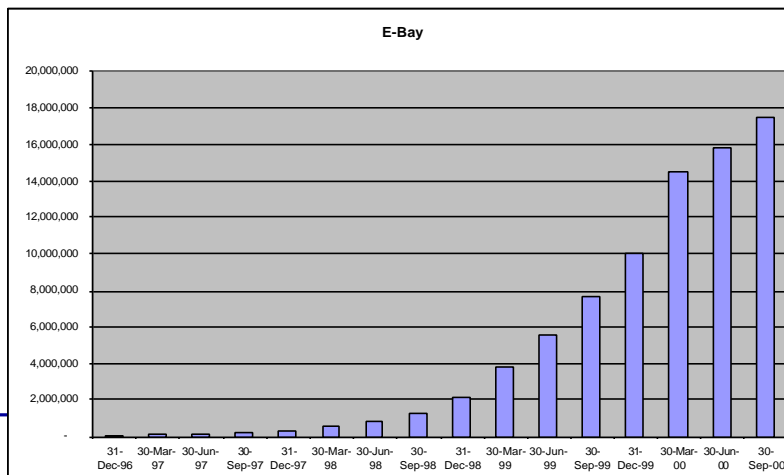


## Number of Customers



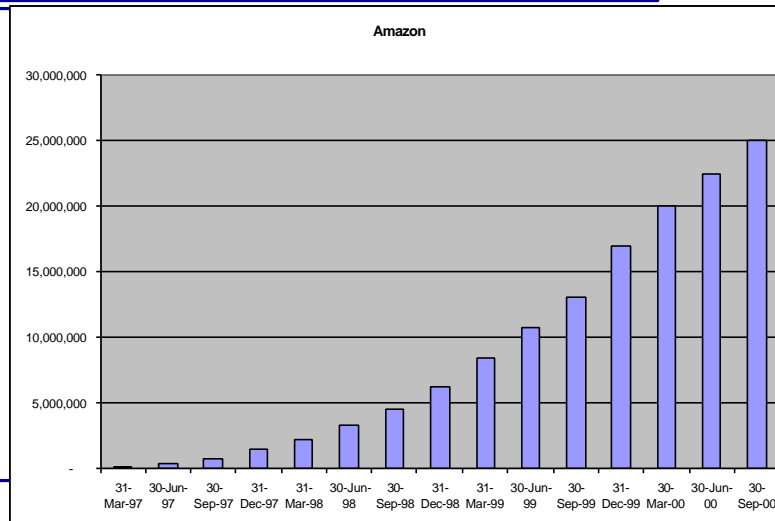
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## Number of Customers



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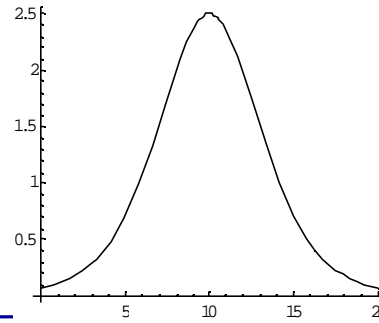
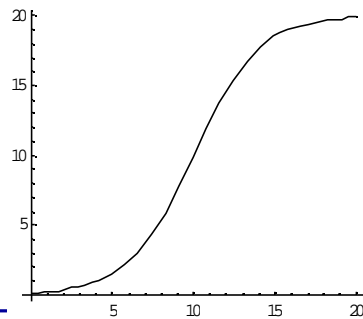
## Number of Customers



## Modeling Number of Customers

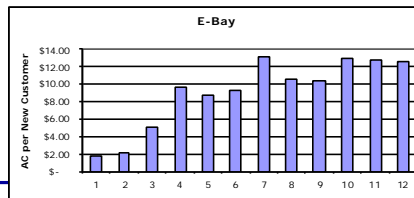
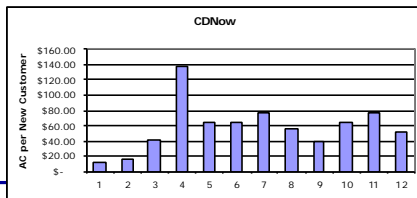
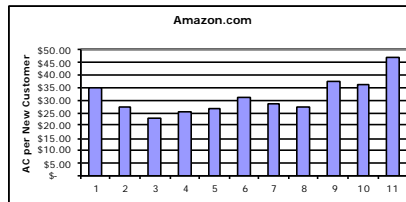
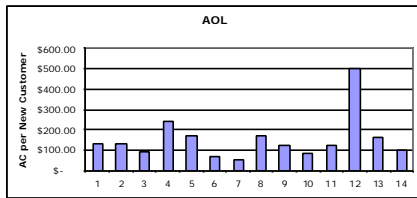
$$N(t) = \frac{a}{1 + \exp(-b - ct)}$$

$$dN(t) = n(t) = \frac{a \cdot c \cdot \exp(-b - ct)}{(1 + \exp(-b - ct))^2}$$



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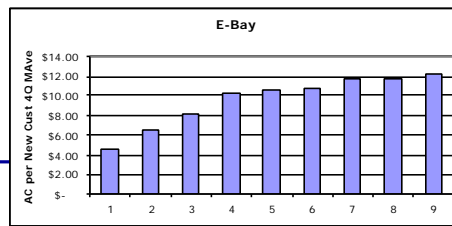
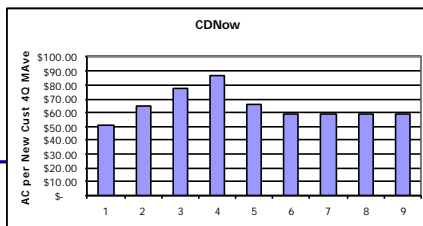
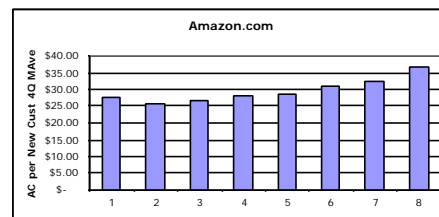
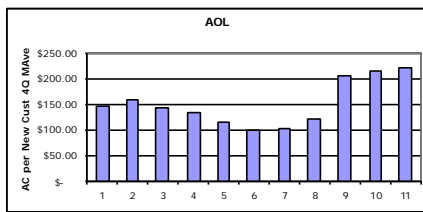
# Acquisition Cost per New Customer



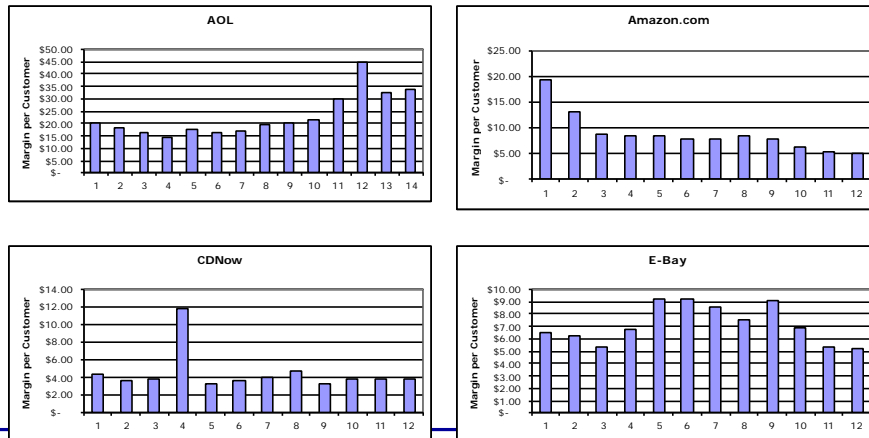
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# Acquisition Cost per New Customer

(4 Qtr Moving Average)

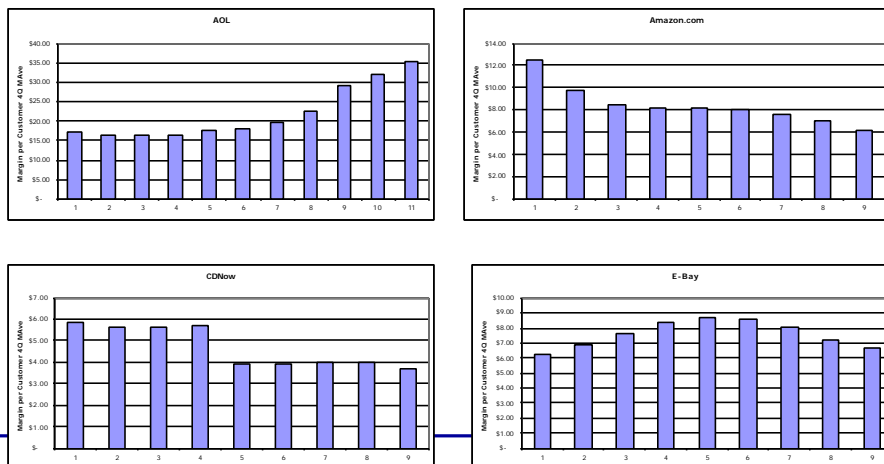


## Margin per Customer



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## Margin per Customer 4 Qtr Moving Average






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## Preliminary Results

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Company	Customers	Margin	AC	Market Cap	Customer Value		
	(Millions)	(\$)	(\$)	(Billions)	60%	70%	80%
	27.88	31.08	31.32	6.00	1.38	1.79	2.38
	3.56	303.88	264.37	2.48	1.71	2.19	2.90
	35.69	132.80	97.60	13.69	11.47	15.57	21.65

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## Issues in Modeling LTV

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- Contractual vs. non-contractual situations
  - Modeling lapsed customers or switchers
  - Models of cross-selling
  - Modeling retention
  - Cost allocations
  - Optimal allocation of resources
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