Supervised Learning for Provenance-Similarity of Binaries

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ABSTRACT
Understanding, measuring, and leveraging the similarity of binaries (executable code) is a foundational challenge in software engineering. We present a notion of similarity based on provenance—two binaries are similar if they are compiled from the same (or very similar) source code with the same (or similar) compilers. Empirical evidence suggests that provenance-similarity accounts for a significant portion of variation in existing binaries, particularly in malware. We propose and evaluate the applicability of classification to detect provenance-similarity. We evaluate a variety of classifiers, and different types of attributes and similarity labeling schemes, on two benchmarks derived from open-source software and malware respectively. We present encouraging results indicating that classification is a viable approach for automated provenance-similarity detection, and as an aid for malware analysts in particular.

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D.2.7 [Software Engineering]: Distribution, Maintenance, and Enhancement—Restructuring, reverse engineering

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Algorithms, Measurement, Security

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Binary Similarity, Classification, Software Provenance

1. INTRODUCTION
Binary similarity is an important area of software engineering research. Techniques for checking binary similarity find applications in areas ranging from code clone detection [18] and software birthmarking [7], to malware analysis [20] and software virology [12]. Several notions of similarity have been proposed and studied in the literature. Our focus is the similarity, which we call provenance-similarity, that arises from the fact that many binaries are the result of compiling “similar” source code with “similar” compilers. The term provenance indicates that the similarity originates not only from the source of the binaries, but also from the (compilation) process by which they were derived.

The major application area for provenance-similarity is malware analysis and virology. Empirical evidence [20] suggests that the vast majority of existing malware belong to a relatively small number of “families” of related instances. For example, a 2006 Microsoft report [3] states that over 97,000 malware variants were detected in the first six months of 2006. At the same time, according to Symantec [19] and Microsoft [3], the typical number of malware families encountered in any six month period is a few hundred. In fact, the Microsoft report (see Figure 1 of [20]) further indicates that the 7 and 25 most common families account for over 50% and 75%, respectively, of detected malware instances.

There are several reasons to believe that many malware families consist of provenance-similar instances. Similarity in source code stems from two factors. First, malware authors reuse old programs—it is very unlikely that the 1,131,335 (presumed) malicious executables with unique MD5 checksums collected by CERT in the final quarter of 2010 were all written from scratch in 92 days. Second, many malware families—such as Aliser [1]—generate new instances by changing a data element (e.g., an encryption key, etc.), but not other parts of the source code. In addition, similarity in generative compilers arises because a small number of related compilers are used to produce the vast majority of malware. For example, we scanned a collection of malware available within CMU CERT and found that of all the malware whose generative compilers are known with reasonable certainty, about 60% were compiled with Microsoft Visual C++, about 25% with Delphi, and most of the rest with Microsoft Visual Basic. Such limited variability in compiler and source code suggests that provenance-similarity is a pervasive feature in malware.

Current approaches to checking provenance-similarity of binaries are largely manual (e.g., forensic analysis done by a malware analyst). While good tools are available for binary disassembly and visualization (e.g., IDAPro [14]), most of the technical analysis is still manual, and, therefore, non-scalable. Automated analysis tools, when available, are either not robust (i.e., they have high false positive and false negative rates) or inefficient. Therefore, developing an automated, robust, and efficient approach for checking provenance-similarity is an important and open problem. Addressing this problem is the subject of our paper.

We begin with a definition of provenance-similarity.
Provenance-similarity between two binaries implies similarity in not only the source code from which they were derived, but also in the compilers used to generate them. We define two binaries $B_1$ and $B_2$ to be provenance-similar if: (i) $B_1$ and $B_2$ have been compiled from the same (or very similar) source code; and (ii) $B_1$ and $B_2$ have been generated by closely related compilers (or the same compilers with different compilation flags).

Note that our definition excludes the situations where the source code of $B_1$ and $B_2$ are very different, such as when $B_1$ is derived from $B_2$ via a major patch, or when $B_1$ and $B_2$ are radically different implementations of the same functionality, e.g., merge-sort and bubble-sort. We also exclude cases where the compilers involved are very different (e.g., Visual C++ versus GCC). These problems are beyond the scope of this paper.

To understand the challenges in detecting provenance-similarity, consider Microsoft Visual C++. As a security feature to guard against buffer-overflow attacks, the compiler is able to generate extra code that checks for stack integrity at runtime, and aborts if an integrity violation is detected. However, the exact code generated depends on the compiler context, which includes factors such as the compilation flags used (e.g., /GS to enable the security feature), the version of the compiler, calling conventions, etc. Consider two binaries, $B_1$ and $B_2$, generated from the same source code by Microsoft Visual C++ under different contexts, and therefore containing different code for runtime buffer-overflow checks. A typical problem is to detect the provenance-similarity of $B_1$ and $B_2$ in a robust and efficient manner.

**Developing a Robust and Efficient Provenance-Similarity Checker.** In the general context of binary similarity, the following two main approaches have been proposed:

(a) **Syntactic** approaches compare signatures [8] or feature vectors [18, 21] extracted from the syntactic binary structure. They resemble techniques used by anti-virus tools, and thus are efficient. However, they are not robust, and are fooled by even minor syntactic differences in binaries.

(b) **Semantic** approaches compute and compare “mathematical” descriptions of the semantic meaning of binaries [11, 15]. They are precise, but require considerable manual interaction, and computationally expensive technology for symbolic and mathematical reasoning (e.g., term-rewriting, symbolic simulation, and theorem proving), and thus have limited practicability and scalability.

In this paper, we investigate the use of classification to develop a robust and efficient binary similarity checker (BSC) for provenance-similarity. Classification is particularly suitable for problems where: (i) closed form solutions are hard to develop, and (ii) a solver can be “learned” using a training set composed of positive and negative samples. Both conditions apply to provenance-similarity.

**Provenance-Similarity as a Classification Problem.** At a high-level, a BSC is a “black box” that accepts a pair of binaries $B_1$ and $B_2$ as input, and outputs “yes” if $B_1$ and $B_2$ are similar, and “no” otherwise. This is clearly a binary classification problem. However, to be effective, a classification-based BSC must be trained properly and use the right classification technology. Moreover, proper training requires good features that are efficiently computable from binaries. We address these challenges, and make the following specific contributions.

**Features.** First, we develop a suite of “semantic” and “syntactic” attributes (a.k.a. features) (cf. Sec. 4). Semantic features capture the effect of a binary’s execution on specific components of the hardware state, viz., registers and memory locations. Syntactic features represent groups of instruction opcodes occurring contiguously in the binary. They are derived from n-grams and n-perms [20]. Second, we extend these features two pairs of binaries to capture the difference between two binaries, and not a single binary in isolation.

**Benchmark.** While malware is a major target domain for provenance-similarity, it is extremely challenging to develop good sample (i.e., training and testing) sets from malware due to the lack of information on source code and generating compilers. Our second contribution is a benchmark (cf. Sec. 5) for provenance-similarity using a benchmark derived from 14 commonly downloaded SourceForge projects, containing more than 21 million LOC.

**Empirical Evaluation.** Finally, we do a systematic evaluation of classification for provenance-similarity over both open-source and malware benchmarks. Our main results are: (i) we compare a suite of classifiers implemented in WEKA [22] on the open-source benchmark, and find RandomForest [4] to be the most effective; (ii) for the malware benchmark, we develop a suite of labeling schemes that do not require source-level information; we show very good classification using these labels and RandomForest; we argue that this implies applicability of classification for provenance-similarity in domains, such as malware, without reliable source-level information; (iii) we compare semantic and syntactic attributes, and show that 1-grams are almost as effective as semantic features, while being much less expensive to compute. Our experiments and results are presented in Sec. 6.

**Function Similarity.** We focus on similarity between binary “functions” instead of complete binaries. Intuitively, a function is a binary fragment that results from the compilation of a procedure or method at the source code level. We choose functions because: (i) they are the smallest externally identifiable units of behavior generated by compilers; (ii) similarity at the function level is desirable for further analysis; indeed, malware of similar provenance, will rarely be identical everywhere, but instead share important functions; thus, malware analysts look for common functions to judge if two binaries are related; also, information about function similarity are useful for clustering and as building blocks for measuring similarity at the binary level; and (iii) we were able to use extensive function-based malware datasets from CERT for our experimentation.

The rest of this paper is structured as follows. In Sec. 2, we survey related work. Sec. 3, we formalize our notion of functions. In Sec. 4, we present our semantic and syntactic features, and the procedures for extracting them from function descriptions. In Sec. 5, we present a benchmark derived from open-source software, and our methodology for deriving testing and training sets from the benchmark. In Sec. 6, we present our experiments and results. In Sec. 7, we conclude.

2. RELATED WORK

A number of different approaches have been proposed for binary similarity. For example, several researchers have used feature vector comparison to detect code clones [18], and to protect against malware [21]. Gao et al. [11] use
a control-flow based analysis that combines graph isomorphism, symbolic simulation, and theorem proving to detect semantic differences in binaries. Apel et al. [2] propose metrics for measuring similarity of malware. Dullien et al. [9] and Flake [10] investigate approaches to compare binaries at the level of graphs derived from their syntax. None of these approaches use supervised learning. Also, they require ultimately the selection of a threshold to decide similarity. In contrast, we use supervised learning to automatically compute a threshold that is appropriate for the target binaries.

Rosenblum et al. [17] propose the use of machine learning to extract compiler provenance from binaries. The goal of compiler provenance is to correctly identify the compiler that was used to generate a target binary. Rosenblum et al. use a specific type of machine learning technology, called the linear chain conditional random field, to discover the most effective solution.

Figure 1: A basic block of an example function, with \( \epsilon \) and \( \pi \) mapping.

Representing Contiguous Functions as Byte-Sequences. Let \( Str \) be the set of finite-length byte sequences (or strings), and \( \cdot \) be concatenation. Let \( \epsilon : Inst \rightarrow Str \) and \( \pi : Inst \rightarrow Str \) be mappings such that: (INJ) \( \epsilon \) is injective, and (PIC) \( \pi(\pi_1) = \pi(\pi_2) \) iff \( \pi_1 \) and \( \pi_2 \) differ only in their address operands. Intuitively, \( \epsilon(\cdot) \) and \( \pi(\cdot) \) are the exact and position-independent representations of \( \cdot \), respectively. For a contiguous function \( f = (Start, Body) \), let \( A = (a_1, \ldots, a_n) \) be the sequence of addresses obtained by sorting \( Dom(Body) \) in increasing order, and \( I = (i_1, \ldots, i_n) \) be the sequence of instructions such that: \( \forall 1 \leq k \leq n \cdot i_k = Body(a_k) \). Then, the exact, \( f.EB \), and position-independent, \( f.PB \), representations of \( f \) are:

\[
\begin{align*}
\ f.EB &= \epsilon(i_1) \cdot \cdots \cdot \epsilon(i_n) \\
\ f.PB &= \pi(i_1) \cdot \cdots \cdot \pi(i_n).
\end{align*}
\]

Example 1. Figure 1 shows a basic block of a function \( f \) with starting address 100025E2, \( Body, \epsilon \) and \( \pi \). Note that while the function starts at 100025E2, the basic block displayed in the figure starts at 100026E3. There are additional addresses in the function both before and after the displayed basic block. The mapping \( \epsilon(\cdot) \) follows the Intel IA-32 instruction definitions, and, thus, satisfies (INJ). The mapping \( \pi(\cdot) \) is obtained by replacing the bytes in \( \epsilon(\cdot) \) which represent address operands with zeros, and, thus, satisfies (PIC). For instructions \( i \) at addresses 100026F9, 10002702, 10002708, and 1000270E, \( \epsilon(\cdot) \neq \pi(\cdot) \) because the operand bytes corresponding to an address have been replaced with zeros in \( \pi(\cdot) \). Instructions at addresses 100026F9, 10002708, and 1000270E have operands which are easily identified as memory dereferences by the type of the operand, while the operands for the instructions at addresses at 100026F3 and 10002702, can only be identified as addresses by the observation that the values of these operands fall inside the defined range of addresses for the program. This heuristic approach is occasionally flawed (e.g., in invalid truncated programs), but we don’t believe this detail is relevant to our results. For all remaining addresses, \( \epsilon(\cdot) = \pi(\cdot) \) since \( \cdot \) does not have any address operands. Finally, \( f.EB \) and \( f.PB \) are, respectively, the concatenation of the elements of the third and fourth columns.

Our approach assumes a reliable way to extract functions from executables. Identifying function boundaries in binaries is a complex and open problem. This is especially true for obfuscated (i.e., packed and/or encrypted) malware. These issues are beyond the scope of this paper.
4. ATTRIBUTES

Recall that our BSC classifies function pairs into two groups—similar (the "yes" group), and dissimilar (the "no" group). We now present our approach to extract attribute vectors from a function pair \((f_1, f_2)\). Since we are interested in the degree of similarity between \(f_1\) and \(f_2\), each attribute captures the difference between \(f_1\) and \(f_2\) along some dimension. More specifically, the attribute vector is constructed as follows:

1. We apply a function-level attribute extraction scheme \(A\) to extract two attribute vectors: \(v_1 = A(f_1)\) and \(v_2 = A(f_2)\). We assume that all attributes extracted by \(A\) are numeric.

2. We construct the attribute vector for \((f_1, f_2)\), denoted by \(A^\Delta(f_1, f_2)\), by taking the pointwise difference of \(v_1\) and \(v_2\). That is:

\[
\forall i \leq |v_1| \cdot A^\Delta(f_1, f_2)[i] = v_1[i] - v_2[i].
\]

Note that \(A^\Delta\) is asymmetric, i.e., in general, \(A^\Delta(f_1, f_2) \neq A^\Delta(f_2, f_1)\). It is possible to make \(A^\Delta\) symmetric by ordering each function pair such that \(f_1.\text{EB} < f_2.\text{EB}\).

We now present two function-level attribute extraction schemes, which we use for our experiments:

1. A semantic approach based on the effect of executing the function on a hardware state.

2. A syntactic approach based on \(n\)-grams and \(n\)-perms [21]—this approach represents existing work on attribute vector extraction from binaries, and serves as a point of comparison. In Sec. 6, we show empirically that classification with semantic attributes outperforms classification with syntactic attributes.

4.1 Semantic Attributes

The semantic attribute vector of a function \(f\), denoted by \(\text{SemAtt}(f)\), is a vector of values of semantic attributes. \(\text{SemAtt}(f)\) represents the effect of executing \(f\) on a state of the hardware. Moreover, semantic attributes are defined so that if \(\text{SemAtt}(f_1)\) and \(\text{SemAtt}(f_2)\) are similar, then the executions of \(f_1\) and \(f_2\) have similar effects. We assume that every function \(f\) has a control flow graph \(f.\text{CFG}\), and that each execution of \(f\) follows a specific path in \(f.\text{CFG}\). The process of extracting a semantic attribute vector from a path in \(f.\text{CFG}\) involves simulation, sign abstraction, and counting abstraction. We now present this process in detail.

4.1.1 Extracting Attribute Vectors from Paths

Let \(\text{SymConst} = \{v_0, v_1, \ldots\}\) be a denumerable set of symbolic constants. Let \(\pm\) denote the set of signs \(\{+,-\}\) and \(N = \{1,2,\ldots\}\) be the set of numerals representing natural numbers. Symbolic expressions, denoted by \(\text{SymExp}\), are linear combinations of symbolic constants (with unit or zero coefficient) and integers. Formally, their syntax has the following BNF form:

\[
\text{SymExp} ::= \pm \text{SymConst} \mid \pm N \mid \pm \text{SymConst} \pm N
\]

**Symbolic State.** Let \(\text{Reg} = \{r_0, r_1, \ldots\}\) be a denumerable set of virtual registers, and \(\text{Mem} = \{m_0, m_1, \ldots\}\) be a denumerable set of memory locations. A symbolic state is a pair \((R,M)\) where: (i) \(R : \text{Reg} \leftrightarrow \text{SymExp}\) maps registers to the symbolic values of their contents; and (ii) \(M : \text{Mem} \leftrightarrow \text{SymExp} \times \text{SymExp}\) maps memory locations to the symbolic values of their addresses and contents.

**Sign Abstraction.** The sign abstraction of a symbolic expression \(e\), denoted by \(\text{Sign}(e)\), is an element of \(\Sigma\), where \(\Sigma = (\pm \cup \{0\}) \times (\pm \cup \{0\}) \setminus \{(0,0)\}\). Intuitively, \(\text{Sign}(e)\) is obtained by removing all symbolic constants and numerals from \(e\), and replacing any missing component with 0. Formally, it is defined as follows:

\[
\text{Sign}(q \cdot v) = (q,0) \quad \text{Sign}(q \cdot n) = (0,q) \quad \text{Sign}(q \cdot v^q \cdot n) = (q,q')
\]

where \(q,q' \in \pm\, v \in \text{SymConst}\), and \(n \in N\). Note that \(\{(0,0)\}\) is not a valid sign abstraction, and \(|\Sigma| = 8\). Sign abstraction extends to pairs of symbolic expressions in the natural manner: \(\text{Sign}(x,y) = (\text{Sign}(x),\text{Sign}(y))\).

**Sign-Abstract State.** Applying sign abstraction to a symbolic state \(s = (R,M)\) results in the sign-abstract state \(\text{Sign}(s)\). Formally, \(\text{Sign}(s)\) is a pair of functions \((R^\#, M^\#)\) such that for \(f = R, M\), the following holds:

\[
\text{Dom}(f) = \text{Dom}(f^\#) \land \forall x \in \text{Dom}(f) : f^\#(x) = \text{Sign}(f(x))
\]

**Counting Abstraction.** Let \(f : X \rightarrow \Sigma\) be any mapping. The counting abstraction of \(f\), denoted by \(\text{Count}(f)\), is the vector of numbers defined as follows. First we order the elements of \(\pm \cup \{0\}\) strictly as: \(- < 0 < +\). This induces the following strict ordering on \(\Sigma\):

\[
(x,y) < (x',y') \iff (x' < x) \lor (x = x' \land y < y')
\]

Let \(\bar{\Sigma}\) be the vector of elements of \(\Sigma\) induced by the above strict ordering on \(\Sigma\). Thus, \(\bar{\Sigma}[1] = (\ldots,-,\ldots)\) and \(\bar{\Sigma}[8] = (+,+,\ldots)\). Then, \(\text{Count}(f)\) is the vector such that:

\[
\text{Count}(f)[i] = |\{x \in X \mid f(x) = \bar{\Sigma}[i]\}|
\]

In other words, the \(i\)-th element of \(\text{Count}(f)\) is the number of elements of \(\text{Dom}(f)\) that are mapped by \(f\) to the \(i\)-th element of \(\bar{\Sigma}\). Note that \(\text{Count}(f)\) always has 8 elements.

For any pair \(x = (x_1,x_2)\), let us write \(\text{Fst}(x)\) and \(\text{Snd}(x)\) to mean \(x_1\) and \(x_2\) respectively. Let \(f : X \rightarrow \Sigma \times \Sigma\) be any mapping. Then the two functions \(\text{Fst}(f)\), \(\text{Snd}(f)\) are defined as follows:

\[
\forall x \in X: \text{Fst}(f)(x) = \text{Fst}(f(x)) \land \text{Snd}(f)(x) = \text{Snd}(f(x))
\]

We write \(\bar{x} \bullet \bar{y}\) to denote the concatenation of vectors \(\bar{x}\) and \(\bar{y}\). The counting abstraction of a sign abstract state \(s^\# = (R^\#, M^\#)\), denoted by \(\text{Count}(s^\#)\), is the vector of numbers defined as follows:

\[
\text{Count}(s^\#) = \text{Count}(R^\#) \bullet \text{Count}(\text{Fst}(M^\#)) \bullet \text{Count}(\text{Snd}(M^\#))
\]

In other words, we apply counting abstraction to the registers, memory addresses, and memory data, and concatenate the resulting vectors. Note that \(\text{Count}(f^\#)\) always has 24 elements. Intuitively, each index of \(\text{Count}(f^\#)\) corresponds to a different a semantic attribute.

**Post-Condition.** A path \(p\) in \(f.\text{CFG}\) is a sequence of assembly instructions. The post-condition of \(p\), denoted by \(\text{Post}(p)\), is a symbolic state representing the hardware configuration after the execution of \(p\). The exact value of \(\text{Post}(p)\) depends on the semantics of the instructions in \(p\). In our experiments, we rely on the ROSE [16] infrastructure to compute \(\text{Post}(p)\).
Example 2. Consider the path $p$ with three instructions `inc ax`, `inc bx`, and `mov [bx] ax`. Thus, $p$ increments register `ax` twice, and then copies the contents of `bx` into the memory location whose addresses are stored in `bx`. Then, $Post(p) = (R, M)$ where:

$$
\begin{align*}
R(r_0) &= +v_0 + 2 \\
R(r_1) &= +v_1 \\
M(m_0) &= (+v_1, +v_0 + 2)
\end{align*}
$$

Note that $r_0$ and $r_1$ represent registers `ax` and `bx`, respectively. Also, $v_0$ and $v_1$ are the initial values of `ax` and `bx`, respectively. Finally, $m_0$ is the memory address whose address is stored in `bx`. Also, $Sign(\text{Post}(p)) = (R^#, M^#)$ where:

$$
R^#(r_0) = (+, +) \quad R^#(r_1) = (+, 0) \quad M^#(m_0) = ((+, 0), (+, +))
$$

Recall that $\Sigma[7] = (+, 0)$ and $\Sigma[8] = (+, +)$. Therefore, $\text{Count}(\text{Sign}(\text{Post}(p))) = \vec{x} \cdot \vec{y} \cdot \vec{z}$, where:

$$
\vec{x}[7] = \vec{x}[8] = \vec{y}[7] = \vec{z}[8] = 1,
$$

and all other elements of $\vec{x}$, $\vec{y}$, and $\vec{z}$ are zero. Extracting Attribute Vectors from Paths. The semantic attribute vector of a path $p$, denoted by $\text{SemAtt}(p)$, is defined as follows:

$$
\text{SemAtt}(p) = \text{Count}(\text{Sign}(\text{Post}(p)))
$$

4.1.2 Extracting Attribute Vectors from Functions

Let $f$ be a function represented by the byte sequence $f.EB$. The attribute vector $\text{SemAtt}(f)$ is constructed from $f.EB$ as follows:

1. $f.EB$ is parsed and the control flow graph $f.CFG$ is constructed. In our implementation, we use the ROSE [16] infrastructure to perform this step.

2. In general, $f.CFG$ has cycles, and therefore infinitely many paths. We use a bounded-depth-first-search traversal to extract $\#p$ paths of depth at most $\#d$ from $f.CFG$. The search is randomized, i.e., successors for traversal are picked randomly. For our experiments, we use $\#p = 50$ and $\#d = 50$. Note that since the number of possible paths is exponential in $\#d$, we limit $\#p$ as well. Let $P$ be the set of paths extracted.

3. From each $p \in P$, we construct $\text{SemAtt}(p)$ as defined in the previous section. Note, $|\text{SemAtt}(p)| = 24$.

4. Let $\cup$ be the element-wise addition of two vectors, i.e.,

$$
\forall i \cdot (\vec{x} \cup \vec{y})[i] = \vec{x}[i] + \vec{y}[i]
$$

Then, we compute $\text{SemAtt}(f)$ as follows:

$$
\text{SemAtt}(f) = \bigcup_{p \in P} \text{SemAtt}(p)
$$

Increasing $\#p$ or $\#d$ also increases the time to extract semantic attributes. Empirically, we found $\#p = 50$ and $\#d = 50$ to be a good tradeoff. For example, to extract semantic attributes from a random sample of 541 functions in our benchmark using $\#p = 50$ and $\#d = 50$, the time required is 95 mins. When $\#d$ is increased to 100, the time is 165 mins, a 74% jump. However, the number of attributes for which values differ between the two cases is only about 1.2% of the total number of attributes.

Example 3. Let $f$ be a function such that $f.CFG$ has two paths $p_1$ and $p_2$. Let $p_1$ be the same as $p$ from Example 2. Therefore, $\text{SemAtt}(p_1) = \text{Count}(\text{Sign}(\text{Post}(p_1))) = \vec{x} \cdot \vec{y} \cdot \vec{z}$, where:

$$
\vec{x}[7] = \vec{x}[8] = \vec{y}[7] = \vec{z}[8] = 1,
$$

and all other elements of $\vec{x}$, $\vec{y}$, and $\vec{z}$ are zero.

Let $p_2$ have 4 instructions `mov [ax] bx`, `dec ax`, `mov bx 10`, `mov [ax] bx`. Then, $Post(p_2) = (R, M)$ where:

$$
\begin{align*}
R(r_0) &= +v_0 - 1 \\
R(r_1) &= +10 \\
M(m_0) &= (+v_0, +v_1) \\
M(m_1) &= (+v_0 - 1, +10)
\end{align*}
$$

Note that $r_0$ and $r_1$ represent registers `ax` and `bx`, respectively. Also, $v_0$ and $v_1$ are the initial values of `ax` and `bx`, respectively. The addresses of memory locations $m_0$ and $m_1$ are stored in `ax` initially and finally, respectively. Also, $\text{Sign}(\text{Post}(p_2)) = (R^#, M^#)$ where:

$$
\begin{align*}
R^#(r_0) &= (+, -) \\
R^#(r_1) &= (0, +) \\
M^#(m_0) &= ((+, 0), (+, +)) \\
M^#(m_1) &= ((+, -), (0, +))
\end{align*}
$$

Recall that $\Sigma[5] = (0, +)$ and $\Sigma[6] = (+, -)$. Therefore, $\text{SemAtt}(p_2) = \text{Count}(\text{Sign}(\text{Post}(p_2))) = \vec{x} \cdot \vec{y} \cdot \vec{z}$, where:

$$
\vec{x}[5] = \vec{x}[6] = \vec{y}[6] = \vec{y}[7] = \vec{z}[5] = \vec{z}[7] = 1,
$$

and all other elements of $\vec{x}$, $\vec{y}$, and $\vec{z}$ are zero. Finally, $\text{SemAtt}(f) = \text{SemAtt}(p_1) \cup \text{SemAtt}(p_2) = \vec{x} \cdot \vec{y} \cdot \vec{z}$, where:

$$
\vec{x}[5] = \vec{x}[6] = \vec{z}[7] = \vec{z}[8] = 1 \\
\vec{y}[6] = 1 \\
\vec{z}[5] = \vec{z}[7] = \vec{z}[8] = 1 \\
\vec{y}[7] = 2
$$

and all other elements of $\vec{x}$, $\vec{y}$, and $\vec{z}$ are zero.

Implementation Details. For our empirical evaluation, we generalize semantic attributes as follows. First, we split registers into three sub-categories: general-purpose, segment, and flag – based on their use by the compiler. We apply sign and counting abstractions separately to each category. Since now there are 3 types of registers in addition to memory addresses and data, $|\text{SemAtt}(p)| = |\Sigma| \times (3 + 2) = 40$ for any path $p$. Second, we consider three ways of combining the elements of $\text{SemAtt}(p)$ to obtain an element of $\text{SemAtt}(f)$ – sum (as described above), minimum, and maximum. We also consider splitting up a path at call-sites, and replacing a counting abstraction with a 0-1 abstraction (i.e., replacing all counts greater than 0 with 1). In all, we have 36 possible combinations, leading to $40 \times 36 = 1440$ attributes.

4.2 Syntactic Attributes

We present two flavors of syntactic attributes, based on n-grams and n-perms [20], respectively. Let $\text{Mnem}$ be the sequence of x86 instruction mnemonics, and $\text{Mnem}^n$ be the set of sequences of $n$ elements drawn from $\text{Mnem}$. Let $\text{Mnem}^n$ be the vector of elements of $\text{Mnem}^n$ ordered lexicographically. For any positive value of $n$, the n-gram vector of $f$, denoted by $\text{NGram}_n(f)$, is computed as follows:

1. Parse $f.EB$ to construct of sequence of assembly instructions $f = (i_1, \ldots, i_k)$. Extract the mnemonic from each instruction to obtain a sequence of mnemonics $M = \langle m_1, \ldots, m_k \rangle$. In our implementation, this step is performed using ROSE.
2. Then, $N\text{Gram}_{n}(f)$ is the vector of $|\text{Mnem}|$ numbers, such that for any $1 \leq i \leq |\text{Mnem}|$, $N\text{Gram}_{n}(f)[i]$ equals the number of times $\text{Mnem}^{n}[i]$ occurs as a subsequence of $M$.

**Example 4.** Let $\text{Mnem} = \{\text{inc}, \text{dec}, \text{mov}\}$. Then, $\text{Mnem}^{2} = \{\text{inc-inc}, \ldots, \text{mov-mov}\}$. Let $f$ be a function such that $f.\text{EB}$ leads to the following sequence of mnemonics: $M = \{\text{mov, inc, inc, mov, dec, mov}\}$. For any $x \in \text{Mnem}^{2}$, let us write $N\text{Gram}_{2}(f)[x]$ to mean $N\text{Gram}_{2}(f)[i]$ such that $\text{Mnem}^{2}[i] = x$. Then,

$$N\text{Gram}_{2}(f)[\text{mov-inc}] = N\text{Gram}_{2}(f)[\text{inc-inc}] = 1$$

$$N\text{Gram}_{2}(f)[\text{inc-mov}] = N\text{Gram}_{2}(f)[\text{mov-dec}] = 1$$

and all other elements of $N\text{Gram}_{2}(f)$ are 0.

For any positive value $n$, the $n$-perm vector of $f$ is denoted by $N\text{Perm}_{n}(f)$. $n$-perm vectors are similar to $n$-gram vectors, except that ordering is ignored.

**Example 5.** For the $\text{Mnem}$ and in Example 4, we have,

$$N\text{Perm}_{2}(f)[\text{inc-mov}] = N\text{Perm}_{2}(f)[\text{dec-mov}] = 2$$

$$N\text{Perm}_{2}(f)[\text{inc-inc}] = 1$$

and all other elements of $N\text{Perm}_{2}(f)$ are 0.

Detailed evaluation of our attributes is presented in Sec. 6.2.

5. TRAINING AND TESTING SETS

Since our training and testing sets are constructed using the same procedure, we refer to them simply as sample sets. A $(N^{+}, N^{-})$-sample set – consisting of $N^{+}$ “yes” samples and $N^{-}$ “no” samples – is constructed as follows:

1. First, we construct a benchmark $B$ comprising of sets of provenance-similar functions.

2. Next, using $B$, we create $N^{+}$ and $N^{-}$ random samples belonging to “yes” and “no” classes respectively. The final result is the union of all the samples obtained.

We now describe these two steps in more detail.

5.1 Benchmark Construction

Our benchmark $B$ consists of a set of clusters, where each cluster is a set of provenance-similar and contiguous functions. $B$ was constructed as follows:

1. We manually selected a set of 14 open-source software packages (containing collectively over 21 million LOC) available at SourceForge (http://www.sf.net) that are among the most downloaded, written in C/C++, and executable on Windows. Each software yielded a set of clusters by the following steps.


3. The binaries were processed with IDAPro 5.6 [14] together with custom Python extensions to extract a set of functions. We write $f.\text{Name}$ to mean the compiler-generated name of a function $f$. We use this name to relate functions across the different compilers, as described in the next step.

4. Recall that $f.PB$ is the position-independent byte-representation of a function $f$. The functions were clustered into equivalence classes induced by the reflexive-transitive closure of the following relation $R$:

$$f_1 R f_2 \iff f_1.\text{Name} = f_2.\text{Name} \lor f_1.PB = f_2.PB$$

Thus, we assume that if $f_1 R f_2$, then $f_1$ and $f_2$ are provenance-similar. Alternatively, we assume that two provenance-dissimilar functions have different names and position-independent byte representations.

5. An equivalence class $c$ was discarded if it satisfied the following condition:

$$|c| = 1 \lor \max_{f \in c}|f.\text{EB}| < 50$$

This eliminates equivalence classes that are: (i) singleton – since, as we see later, singletons are not useful in generating “yes” samples; and (ii) have no functions with bodies larger than 50 bytes – since we believe that classification is not applicable to detect similarity between very small functions. The cutoff of 50 was chosen empirically.

6. Each remaining equivalence class yields a cluster.

Table 1 summarizes our benchmark $B$. A median of (mostly) 3 indicates that the most common case is, as expected, one function for each of the 3 compilers. The number of equivalence classes, averages and standard deviations vary widely, indicating that we have a good mix of clusters in terms of their sizes.

5.2 Sample Set Construction

We now present our approach to construct a $(N^{+}, N^{-})$-sample set from $B$. When constructing (either “yes” or “no”) samples, we ignore function pairs $(f_1, f_2)$ such that $f_1.PB = f_2.PB$1, since, by assumption, such function pairs

<table>
<thead>
<tr>
<th>Software</th>
<th>KLoC</th>
<th>BSz</th>
<th>#Cl</th>
<th>Avg</th>
<th>StD</th>
<th>Med</th>
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<td>2992</td>
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<td>9.4</td>
<td>3</td>
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<td>7.8</td>
<td>3</td>
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<td>1507</td>
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<tr>
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<td>3</td>
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<td>1.4</td>
<td>639</td>
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<tr>
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<td>27.3</td>
<td>1646</td>
<td>9.8</td>
<td>63.8</td>
<td>3</td>
</tr>
</tbody>
</table>

1Without this restriction, the overall trend in our results is similar, but with even higher $F$-measures.
are already provenance-similar, and hence need not be classified. In the following, $\Psi$ is a scheme to extract feature vectors from function pairs, as described in Sec. 4.

First, to construct a “yes” sample, we use procedure PickYes, consisting of the following steps: (i) Randomly pick a cluster $c \in \mathcal{B}$. Recall that $c$ contains at least two functions. (ii) Randomly pick two distinct functions $f_1, f_2$ s.t. $f_1, PB \neq f_2, PB$. (iii) Output $\Psi(f_1, f_2)$ labeled with “yes”. Next, to construct a “no” sample, we use procedure PickNo, consisting of the following steps: (i) Randomly pick two distinct clusters $c_1, c_2 \in \mathcal{B}$. (ii) Randomly pick two functions $f_1 \in c_1$ and $f_2 \in c_2$. (iii) Output $\Psi(f_1, f_2)$ labeled with “no”. Finally, to construct the desired $(N^+, N^-)$-sample set, we repeat PickYes $N^+$ times, PickNo $N^-$ times, and collect together the resulting samples.

The benchmark $\mathcal{B}$ consists of over six million functions, divided into 17,852 clusters. Therefore, we have over $36 \times 10^{12}$ possible samples available for training and testing. In our experiments, we use sample sets consisting of an equal proportion of “yes” and “no” samples. Thus, we say “$(n_1, n_2)$-classification” to mean a classification with a $(\frac{n_1}{n_2}, \frac{n_2}{n_1})$-training set, and a $(\frac{n_1}{n_2}, \frac{n_2}{n_1})$-testing set.

Since our testing and training sets are randomly created, we repeat our experiments several times, and use the averages of the measurements for our conclusions. Specifically, for any metric $M$, we say “$M$ of $(n_1 \times k_1, n_2 \times k_2)$-classification” to mean the average of the values of $M$ for $n_1 \times k_1$ -classifications, done by: (i) selecting $k_1$ random training sets of size $n_1$, and for each training set, (ii) learning a classifier and testing it with $k_2$ random testing sets of size $n_2$. We use three main metrics for our evaluation – the F-measure, training time, and testing time.

6. EXPERIMENTAL RESULTS

We performed three types of experiments: learner selection, feature selection, and to judge the applicability of our approach to detect similarity in malware. All experiments were performed on a quad-core 2.8 GHz machine. Each session (training or testing) was run with a time limit of 1800s and a memory limit of 700MB. Our benchmark and tools are available at http://www.contrib.andrew.cmu.edu/user/schaki/binsim.

6.1 Learner Selection

These experiments were done with the semantic attributes – i.e., with $\Psi = \text{SemAtt}\Delta$ – on our open-source benchmark $\mathcal{B}$. We first evaluated 24 classifiers implemented in the WEKA [22] tool (version 3.6.2). For each classifier, we used the default WEKA configuration, and measured $F$ for a $(10000 \circ 5, 20000 \circ 5)$-classification. We observed a clear separation between the classifiers: seven are effective – having $F$-measures $\geq 0.875$; the rest are ineffective – having $F$-measures around $\approx 0.5$ (like random guessing). The results for the 7 effective schemes, in order of decreasing $F$-measure, are summarized in Table 2.

Comparing Effective Schemes. Next, we compared the performance of the 7 effective schemes. The IBk and J48graft schemes are eliminated immediately. They have worse performance – lower $F$-measure, and higher training and testing times – compared to RandomForest. We evaluated each of the remaining 5 schemes using a series of $(N \circ 5, 2N \circ 5)$-classifications, where the value of $N$ was varied from 10000 to 30000 in increments of 2000. The results are summarized in Figure 2. All classifiers show increasing $F$-measures with increasing $N$. However, RandomForest is the clear winner. All classifiers also require more testing and training time with increasing $N$. In particular, Ridor’s training is most expensive, and it times out for training sets of size 24,000 and up. Overall, we conclude that RandomForest is the most effective classifier.

RandomForest. Next, we evaluated RandomForest by varying its three parameters – (P1) number of trees, (P2) number of attributes, and (P3) tree depth.

First, we performed $(N \circ 5, 2N \circ 5)$-classifications with increasing P1, and with $N$ ranging from 5 to 150. Figure 3-(top) summarizes the $F$-measures we observed. The $F$-measure improves rapidly with increasing P1 up to $N = 20$, then improves very slowly till $N = 40$. For $N > 40$, the improvement tapers off, and is difficult to ascertain.

Next, we performed $(N \circ 5, 2N \circ 5)$-classifications with increasing P2, and with different $N$. Figure 3-(bottom) summarizes the $F$-measures we observed. As expected, the $F$-measure improves with increasing P2, but the gains taper off after about 12.

Finally, we performed $(N \circ 5, 2N \circ 5)$-classifications with increasing P3 – starting at 0 (which indicates unlimited depth), and moving up to 80 in increments of 10 – and with different $N$. We saw that P3 $\geq 20$ is required for an $F$-measure within 0.1 of the $F$-measure with unlimited P3. However, at P3 = 20, the training and testing times are similar to those with unlimited P3. Therefore, unlimited P3 is the optimal choice.

In all cases, training and testing times increase monotonically with the values of P1, P2, P3, and $N$.

6.2 Feature Selection

Next, we compared $\text{SemAtt}\Delta$, $\text{NGram}_n\Delta$ and $\text{NPerm}_n\Delta$ for $n = \{1, 2\}$ using our open-source benchmark $\mathcal{B}$. We evaluated their performances using a series of $(N \circ 5, 2N \circ 5)$-classifications, where the value of $N$ was varied from 10000 to 30000 in increments of 2000. Table 3 shows our results. We see that $\text{NGram}_1\Delta$ is superior to $\text{SemAtt}\Delta$ in terms of training and testing times, and almost as good in terms of $F$-measure. Feature extraction with $\text{NGram}_1\Delta$ is also less expensive than $\text{SemAtt}\Delta$ (e.g., about one day vs. a week for our open-source benchmark). A combination of $\text{SemAtt}\Delta$ and $\text{NGram}_1\Delta$ improves negligibly over $\text{SemAtt}\Delta$ alone.

As expected, classification with $\text{NGram}_2\Delta$ and $\text{NPerm}_2\Delta$ is slower than with $\text{NGram}_1\Delta$ due to a greater number of attributes. However, surprisingly, it is.

Table 2: Comparison of various classifiers on a $(10000 \circ 5, 20000 \circ 5)$-classification. $F$-measure $= \text{avg/stdev}$; Train = training time (avg/stdev in secs); Test = testing time (avg/stdev in secs).

<table>
<thead>
<tr>
<th>Classifier</th>
<th>$F$-measure</th>
<th>Train</th>
<th>Test</th>
</tr>
</thead>
<tbody>
<tr>
<td>RandomForest</td>
<td>0.928/0.002</td>
<td>19.41/0.23</td>
<td>4.56/0.075</td>
</tr>
<tr>
<td>J48graft</td>
<td>0.909/0.002</td>
<td>97.96/6.28</td>
<td>6.52/0.301</td>
</tr>
<tr>
<td>J48</td>
<td>0.900/0.003</td>
<td>93.74/4.95</td>
<td>3.34/0.056</td>
</tr>
<tr>
<td>RIDOR</td>
<td>0.892/0.005</td>
<td>266.7/27.1</td>
<td>2.79/0.045</td>
</tr>
<tr>
<td>REPTree</td>
<td>0.887/0.003</td>
<td>22.15/0.64</td>
<td>3.08/0.044</td>
</tr>
<tr>
<td>RandomTree</td>
<td>0.876/0.003</td>
<td>5.72/0.13</td>
<td>3.89/0.123</td>
</tr>
<tr>
<td>IBk</td>
<td>0.861/0.003</td>
<td>164.6/2.97</td>
<td>459.0/26.6</td>
</tr>
</tbody>
</table>
also worse in terms of F-measure. This indicates that counts of pairs of adjacent instruction mnemonics characterize a function less well than the counts of single mnemonics. We believe that one reason for this is instruction reordering due to compiler optimizations and changes in source code, the two sources of provenance similarity. The same set of instructions, upon reordering, will lead to different \textit{NGram}_\Delta and \textit{NPerm}_\Delta, but the same \textit{NGram}_1. Overall, we believe \textit{NGram}_1 is the best choice if time is limited, and \textit{SemAtt}_\Delta is best otherwise.

Recall that \(\textit{A}^\Delta\) computes the element-wise difference of function-level attribute vectors. We also evaluated \(\textit{A}^\Delta\) against another approach – denoted by \(\textit{A}^*\) – that simply concatenates the two function-level vectors. Specifically,

\[
\textit{A}^*(f_1, f_2) = \textit{A}(f_1) \bullet \textit{A}(f_2) \quad (\bullet \text{ denotes concatenation})
\]

Note that \(\textit{A}^*(f_1, f_2)\) has more attributes than \(\textit{A}^\Delta(f_1, f_2)\), and captures information about the difference between \(f_1\) and \(f_2\) less directly. Empirically, we found \textit{SemAtt}_\Delta to be superior to \textit{SemAtt}_*, as shown in Table 3.

### 6.3 Applicability to Malware

To judge the applicability of classification to detect similarity in malware, we experimented with a benchmark \textit{M} derived from 12 malware families from the CERT database. To ensure that we only consider true families, we picked a dozen candidates from cases on which a suite of anti-virus tools all agree in their family identification. The details of the families are presented in Table 4.

The main problem with malware is designing a good labeling function for training provenance-similarity. Since source-level information is rarely available, it is difficult to automatically decide if two functions are similar (or not) with high confidence. While the labeling problem for malware is beyond the scope of our paper, as a starting point, we experimented with a labeling function – denoted \(L^{PIC}\) – based on position-independent (PIC) byte representations. Specifically, \(L^{PIC}\) labels an attribute vector derived from a function pair \((f_1, f_2)\) “yes” iff \(f_1\) and \(f_2\) have the same PIC byte representation. We don’t claim that \(L^{PIC}\) is the best possible labeling function for malware similarity. However, we believe that it is a good approximation to the extent that if classification with \(L^{PIC}\) is not accurate, it will likely be inaccurate with a better labeling function as well.

We created sample sets using our benchmark \textit{M} and \(L^{PIC}\), and performed a series of \((N\leq 5, 2N\leq 5)\)-classifications, where the value of \(N\) was varied from 10000 to 30000 in increments of 2000. We repeated our experiments with
Table 3: Comparison of $\text{SemAtt}^\Delta$, $\text{NGram}_1^\Delta$, and $\text{SemAtt}^*$; $SA + NG_1 = \text{SemAtt} + \text{NGram}_1$; $N$ = size of training set; $Tr = \text{Avg. training time (s)}$; $Te = \text{Avg. testing time (s)}$.

<table>
<thead>
<tr>
<th>$N$</th>
<th>$\text{SemAtt}^\Delta$</th>
<th>$\text{NGram}_1^\Delta$</th>
<th>$(SA + NG_1)^\Delta$</th>
<th>$\text{NGram}_2^\Delta$</th>
<th>$\text{NPerm}_2^\Delta$</th>
<th>$\text{SemAtt}^*$</th>
</tr>
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<tbody>
<tr>
<td>10K</td>
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<td>0.919</td>
<td>0.930</td>
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<tr>
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<td>0.889</td>
<td>0.900</td>
</tr>
<tr>
<td>14K</td>
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<td>0.935</td>
<td>0.894</td>
<td>0.894</td>
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<td>0.925</td>
<td>0.936</td>
</tr>
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</table>

$\text{SemAtt}^\Delta$ and $\text{NGram}_1^\Delta$. In all cases, we got a high $F$-measure (0.998), indicating that classification is a promising approach for provenance-similarity in malware.

7. CONCLUSION

In this paper, we explore the use of classification to detect provenance-similarity of binaries. Specifically, we use classification to predict if a pair of functions is “similar” or “dissimilar”. Our classification uses features that capture the difference between the target function pair. We evaluate our approach on a benchmark derived from open-source software, with encouraging results. Preliminary experiments also indicate that classification is a promising approach to detect malware similarity. A major challenge with malware is the difficulty of obtaining sufficiently many samples with reliable similarity labeling. We believe that semi-supervised learning is a promising avenue in addressing this issue.

8. REFERENCES